

# Consideration of Inter-Pulse and Intra-Pulse Satellite Motion in Zero Doppler SAR Processing

Ulrich Balss, Helko Breit, Michael Eineder

Remote Sensing Technology Institute (IMF)  
German Aerospace Center (DLR)

November 9th, 2017



Knowledge for Tomorrow



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.
- **Here, I discuss:**



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.
- **Here, I discuss:**
  - Which of the motion effects are in need to be corrected for.



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.
- **Here, I discuss:**
  - Which of the motion effects are in need to be corrected for.
  - What is the amount of these effects.



# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.
- **Here, I discuss:**
  - Which of the motion effects are in need to be corrected for.
  - What is the amount of these effects.
  - Where is the adequate place in processing chain to correct for them.





# Introduction

- In recent years:
  - Several studies showed that pixel location accuracy at centimeter level is attainable.
- Prerequisite:
  - Tight quality standards throughout entire processing chain
- Aiming at centimeter accuracy level:
  - Processor approximations in SAR focusing have to be reassessed.
  - In particular, Stop-Go-Approximation is challenged.
- **Here, I discuss:**
  - Which of the motion effects are in need to be corrected for.
  - What is the amount of these effects.
  - Where is the adequate place in processing chain to correct for them.
  - What is the attainable gain in location accuracy.
    - (based on Sentinel-1 and TerraSAR-X examples)



# Inter-Pulse and Intra-Pulse Satellite Motion

## Inter-Pulse Motion

From pulse transmission to echo reception

## Intra-Pulse Motion

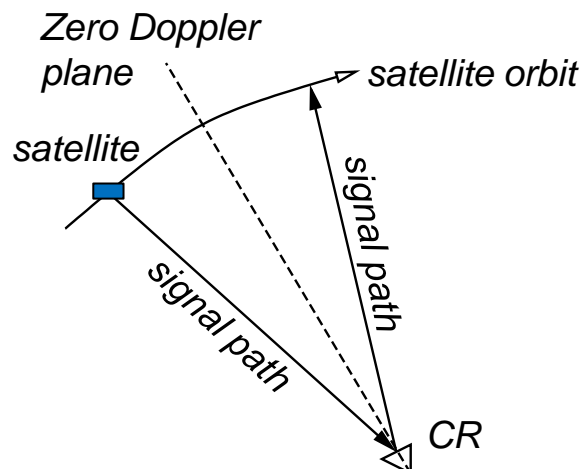
During echo reception

## Intra-Pulse Motion

During pulse duration

## Inter-Pulse Motion

Increase of signal travel distance



# Inter-Pulse and Intra-Pulse Satellite Motion

Inter-Pulse  
Motion

From pulse  
transmission to  
echo reception

Intra-Pulse  
Motion

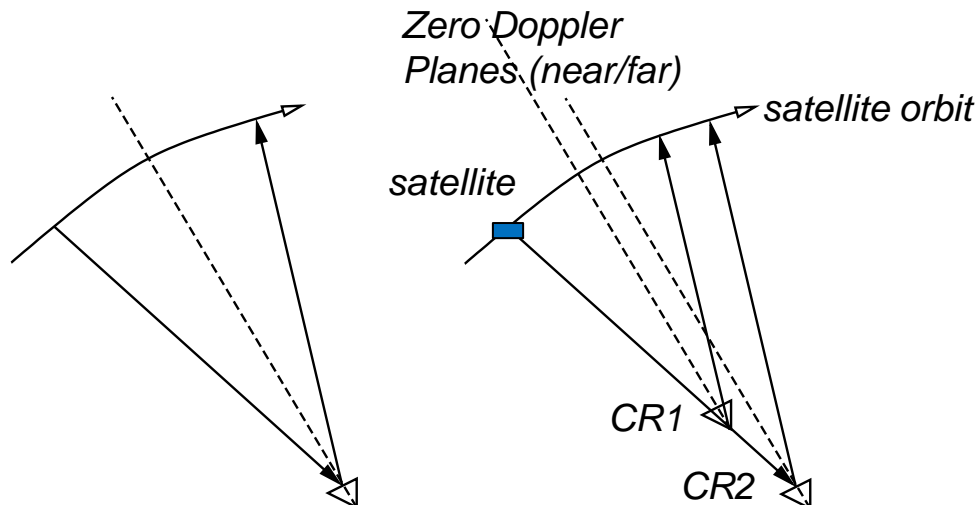
During echo  
reception

Intra-Pulse  
Motion

During pulse  
duration

Inter-Pulse  
Motion

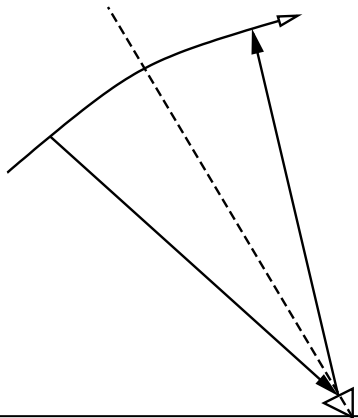
Increase of  
signal travel  
distance



# Inter-Pulse and Intra-Pulse Satellite Motion

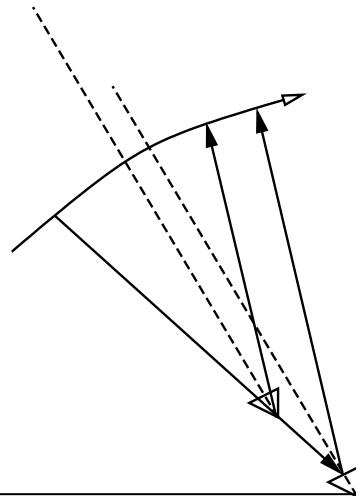
## Inter-Pulse Motion

From pulse transmission to echo reception



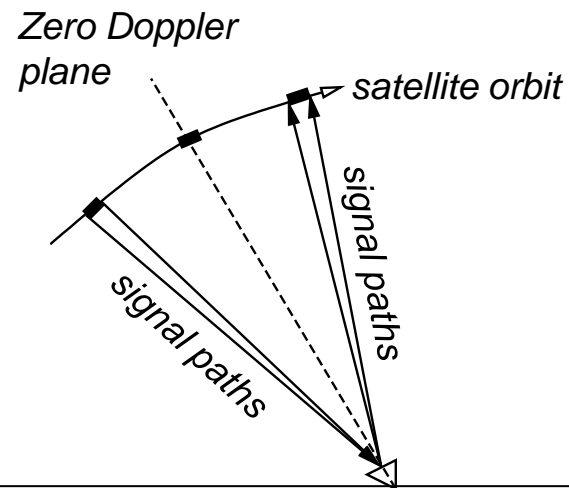
## Intra-Pulse Motion

During echo reception



## Intra-Pulse Motion

During pulse duration



## Inter-Pulse Motion

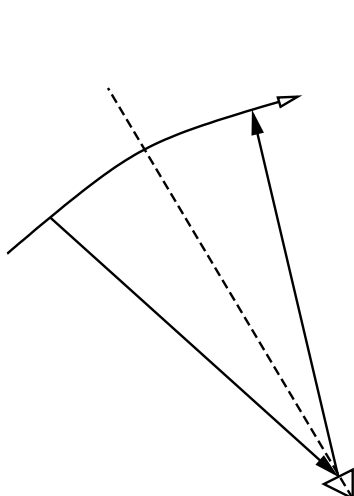
Increase of signal travel distance



# Inter-Pulse and Intra-Pulse Satellite Motion

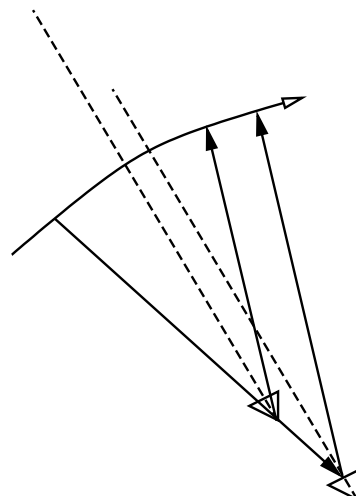
## Inter-Pulse Motion

From pulse transmission to echo reception



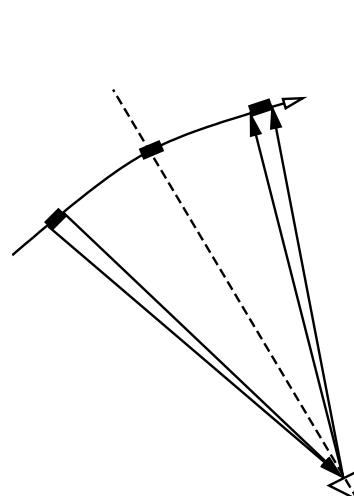
## Intra-Pulse Motion

During echo reception



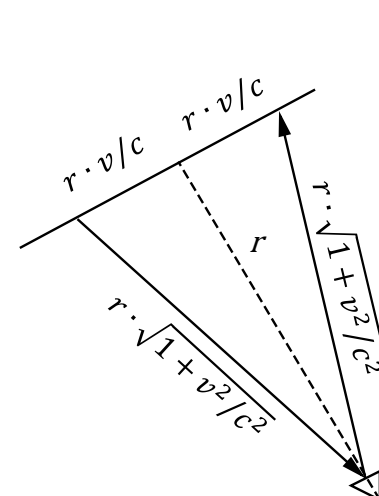
## Intra-Pulse Motion

During pulse duration



## Inter-Pulse Motion

Increase of signal travel distance



# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	—	(30 – 40 m)	—
Motion during echo reception	0.6 – 5.2 m	—	(0.04 – 3.8 m)	—
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	—	0.15 – 0.25 mm	—	(0.15 – 0.25 mm)

Embraced values mean that the respective effect is already considered in SAR processor (*operational* IPF or TMSP).



# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	—	(30 – 40 m)	—
Motion during echo reception	0.6 – 5.2 m	—	(0.04 – 3.8 m)	—
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	—	0.15 – 0.25 mm	—	(0.15 – 0.25 mm)

Motion from pulse transmission to echo reception is considered by both SAR processor (IPF and TMSP).



# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	–	(30 – 40 m)	–
Motion during echo reception	0.6 – 5.2 m	–	(0.04 – 3.8 m)	–
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	–	0.15 – 0.25 mm	–	(0.15 – 0.25 mm)

Motion during echo reception is consider by TMSP only.





# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	–	(30 – 40 m)	–
Motion during echo reception	0.6 – 5.2 m	–	(0.04 – 3.8 m)	–
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	–	0.15 – 0.25 mm	–	(0.15 – 0.25 mm)

Motion during pulse duration is considered by TMSP only.  
(\* = secondary effect in range)



# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	—	(30 – 40 m)	—
Motion during echo reception	0.6 – 5.2 m	—	(0.04 – 3.8 m)	—
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	—	0.15 – 0.25 mm	—	(0.15 – 0.25 mm)

Increase of signal travel distance is considered by TMSP  
(Spin-off from bistatic TanDEM mission).



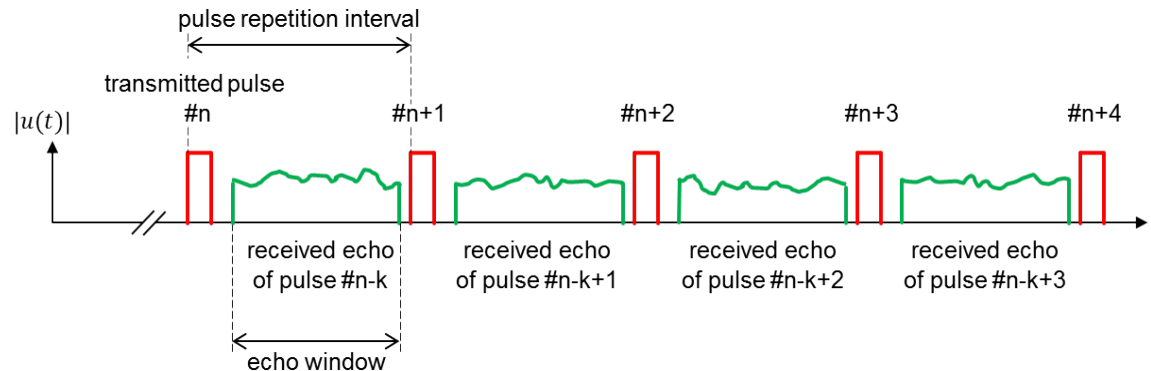
# Amount of Effects in Case of Sentinel-1 and TerraSAR-X

Effect	Sentinel-1 azimuth	Sentinel-1 range	TerraSAR-X azimuth	TerraSAR-X range
Motion from pulse transmission to echo reception	(30 – 40 m)	—	(30 – 40 m)	—
Motion during echo reception	0.6 – 5.2 m	—	(0.04 – 3.8 m)	—
Motion during pulse duration	0.2 – 0.45 m	0.00 – 0.75 m*	(0.2 – 0.45 m)	(0.00 – 0.01 m)*
Increase of signal travel distance	<b>This effect is negligible so far!</b>			

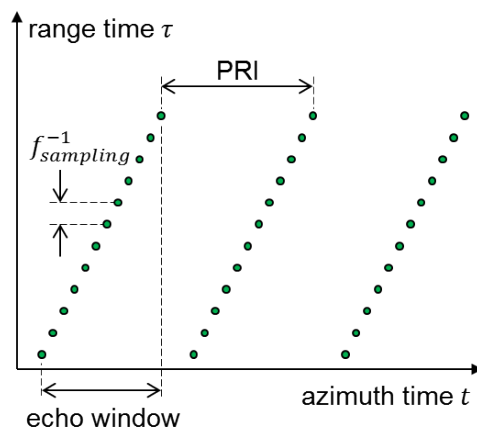


# Consequences of Satellite Motion on Raw Data

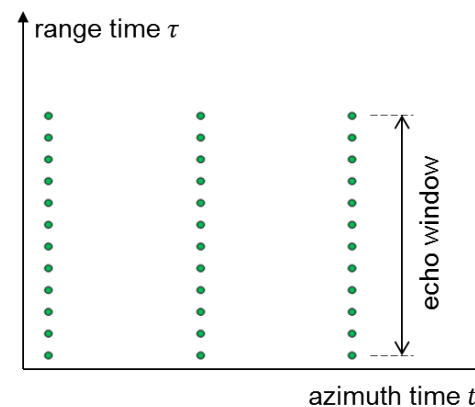
## Contiguous echo data stream



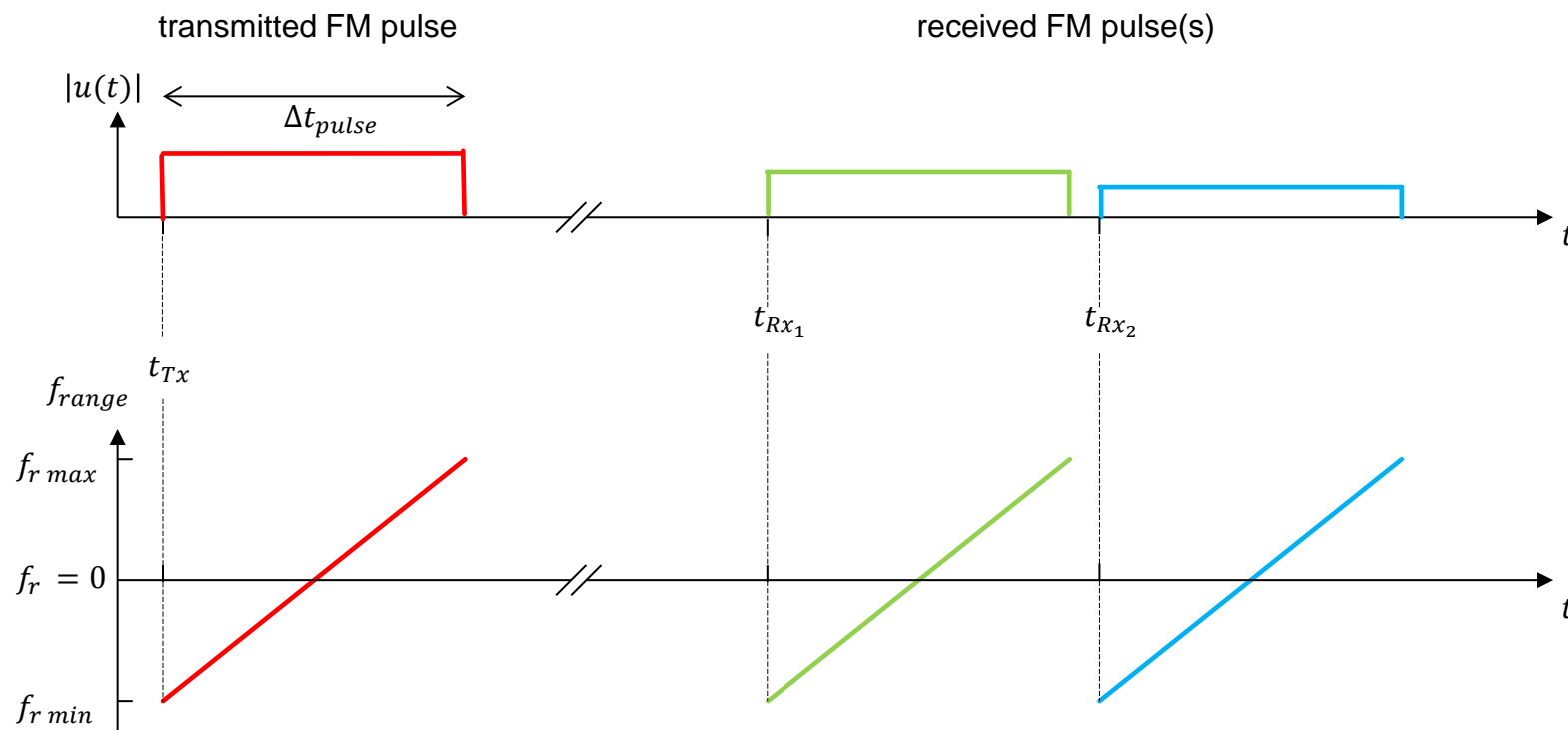
True timing of 2-D  
echo sample matrix



Timing, assumed by  
Stop-Go-Approximation

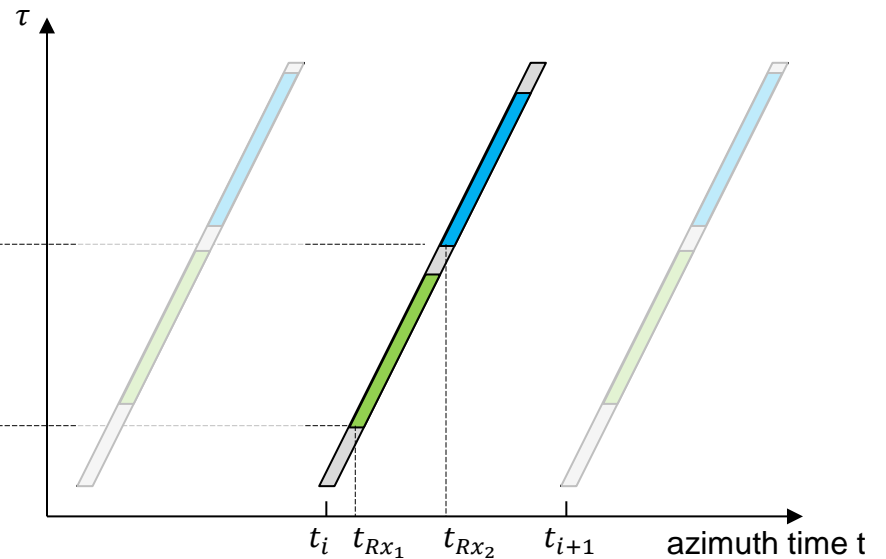
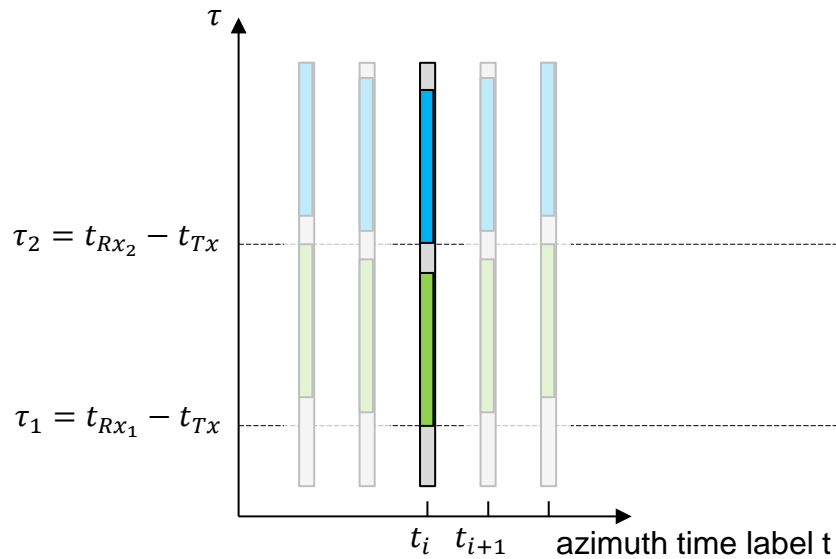


A pulse transmitted at  $t_{Tx}$ , scattered back from a ground target with a signal round trip time  $\tau_{delay} = t_{Rx} - t_{Tx}$  is received at azimuth time  $t_{Rx}$



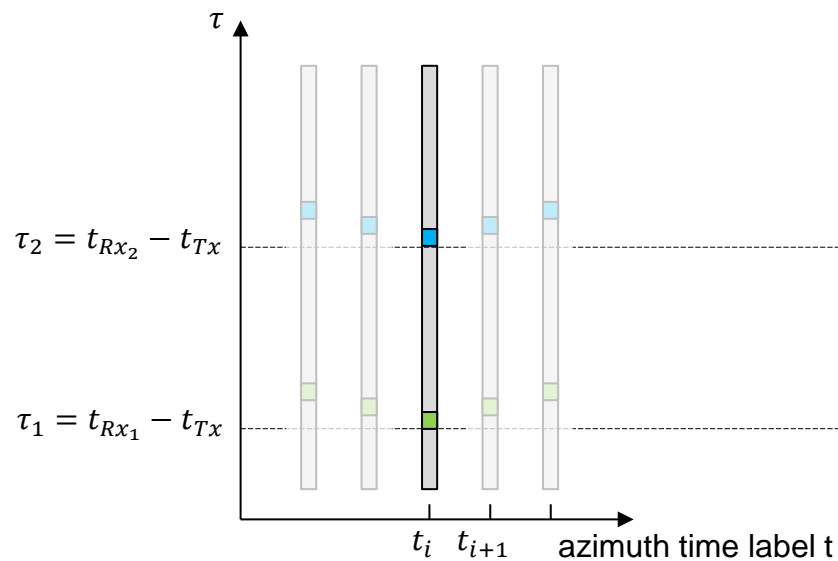
SAR raw data matrix with  
stop & go azimuth time labels

**true** azimuth timing of  
SAR raw data matrix

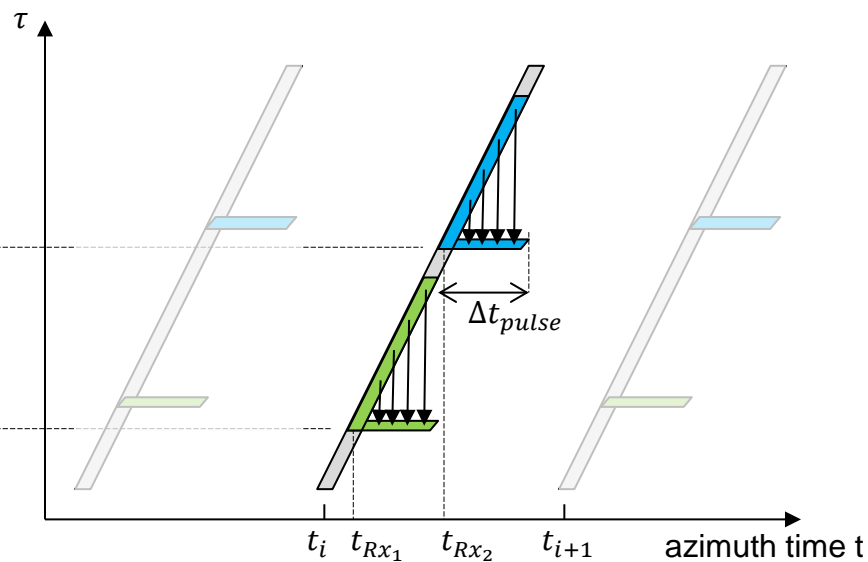


# Pulse Compression

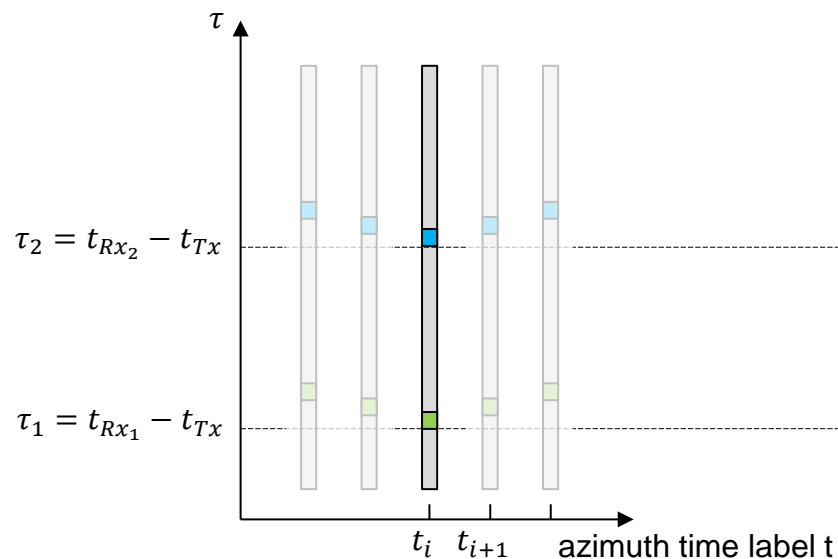
SAR raw data matrix with  
stop & go azimuth time labels



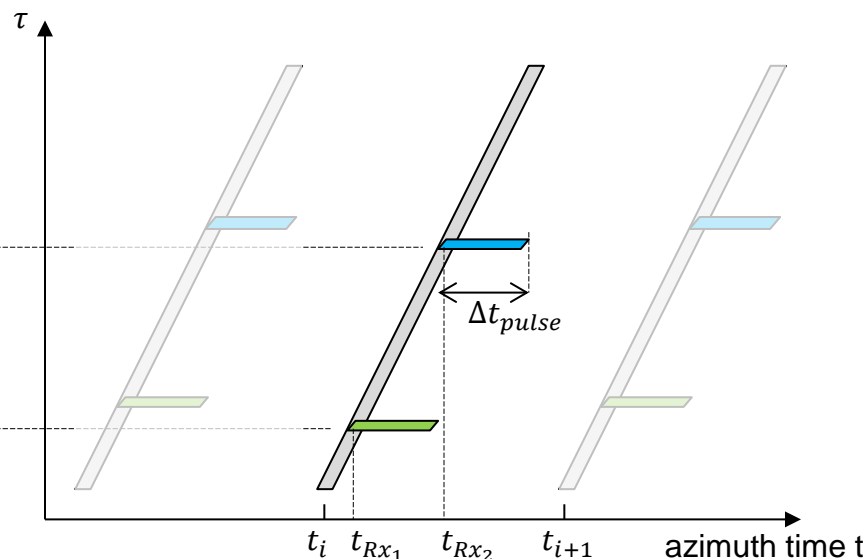
**true** azimuth timing of  
SAR raw data matrix



SAR raw data matrix after pulse  
compression with  
stop & go azimuth time labels



true azimuth timing of  
SAR raw data matrix after pulse  
compression



without correction of intra pulse motion range  
compressed data is smeared out in azimuth by  
the pulse duration  $\Delta t_{pulse}$



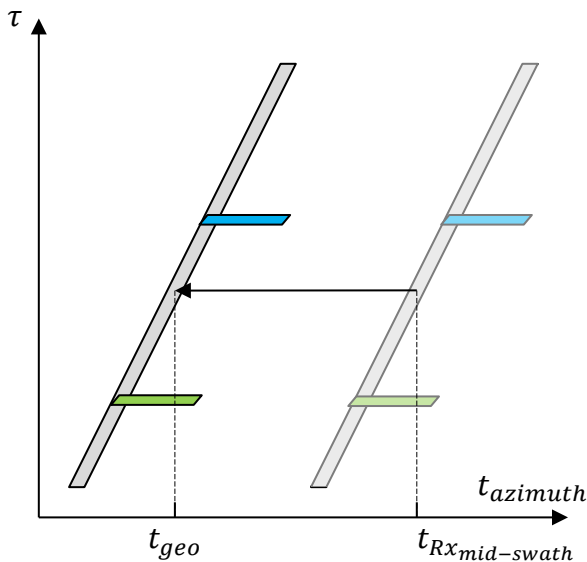


# Levels of Stop & Go Correction

## Sentinel 1:

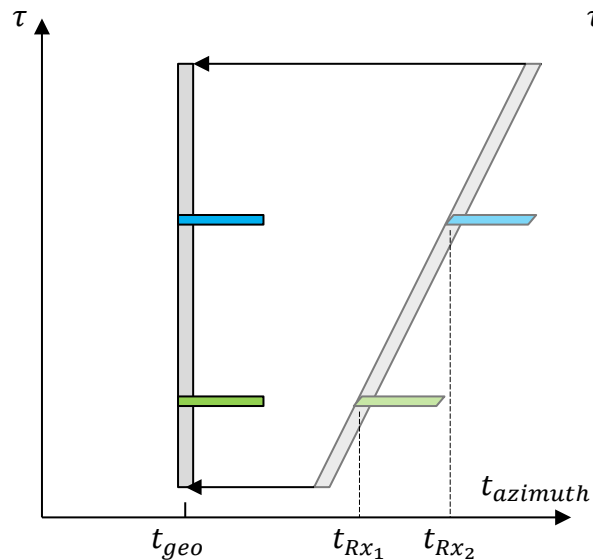
### Partial stop & go correction:

- Inter pulse motion @ mid swath



### Partial stop & go correction:

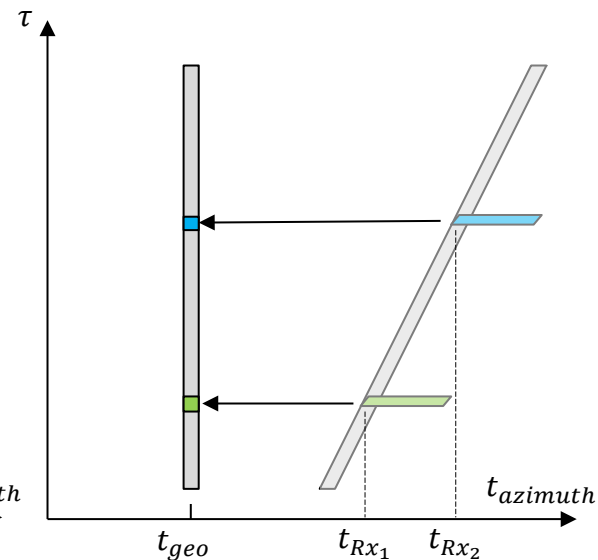
- Inter pulse motion



## TerraSAR-X:

### Complete stop & go correction:

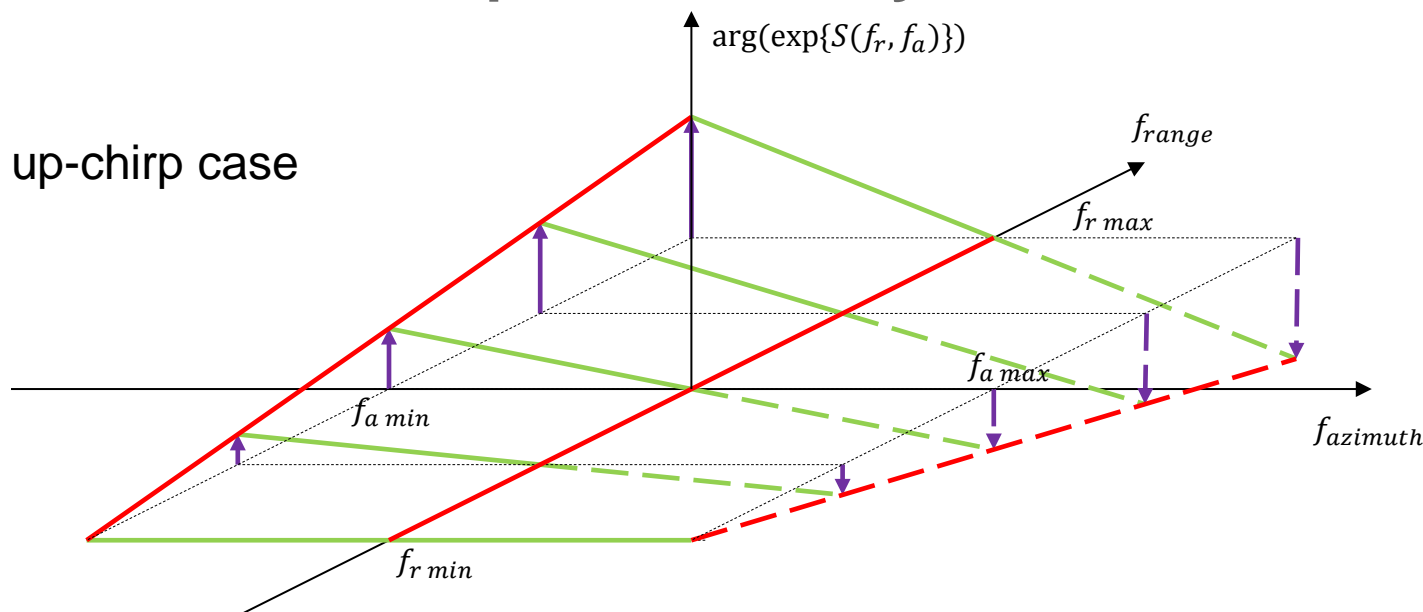
- Inter pulse motion
- Intra pulse motion



$t_{geo}$  defines the time instant where the line of sight – satellite to target vector – is perpendicular to the flight trajectory and the zero-Doppler condition is fulfilled in a geometrical sense



# Spectral Phase Slopes caused by Intra Pulse Motion



- $f_{\text{range}}$ -dependent azimuth time offsets cause **spectral azimuth phase ramps** (green)
- **Spectral azimuth phase ramps** cause **spectral range phase ramps** (red)
- **Spectral range phase ramps** cause  $f_{\text{azimuth}}$ -dependent range time offsets

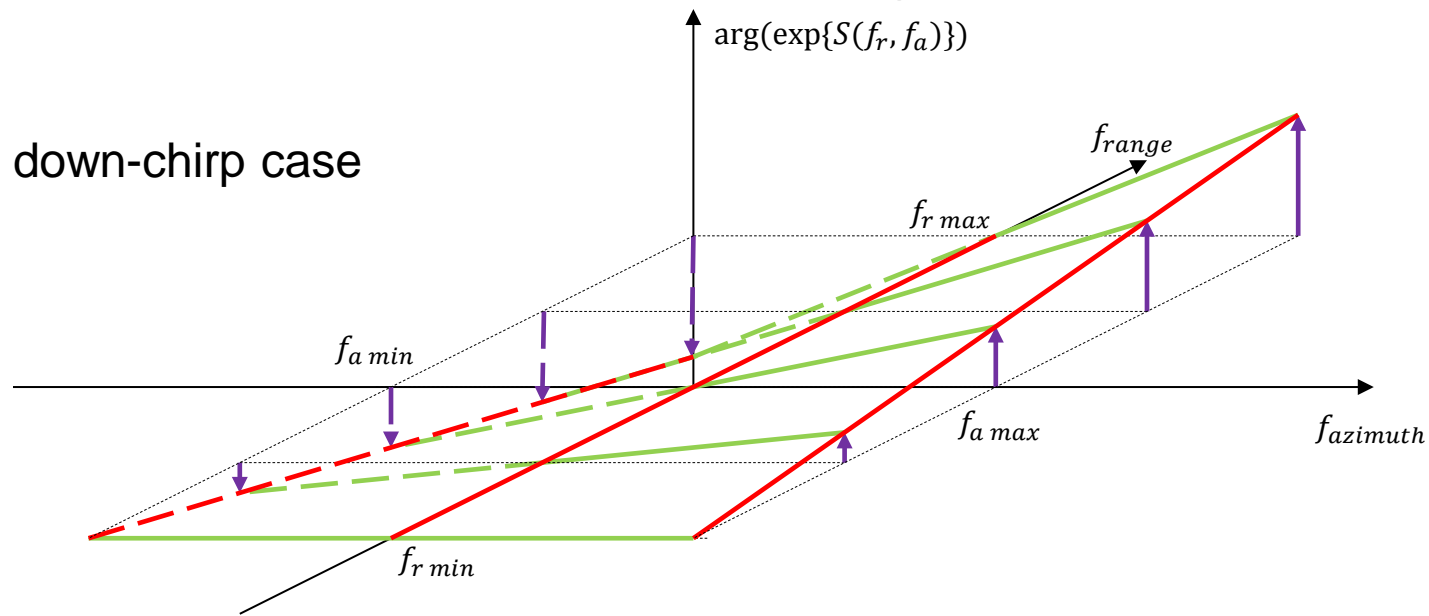
⇒ Stripmap Mode:

negative & positive spectral phase slopes sum up to defocusing (dm-level) but do not cause residual time offsets.

⇒ TOPS Mode: defocusing + DopCen-dependent range time offsets



# Spectral Phase Slopes caused by Intra Pulse Motion



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$

**In case of Sentinel-1 data : reference not at mid range  
(Confirming previous observations made by Aresys)**



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$

**In case of Sentinel-1 data : reference not at mid range  
(Confirming previous observations made by Aresys)**

- Intra-pulse motion during pulse duration:

$$\tau \rightarrow \tau - \frac{f_{\text{DC}}}{K_r}$$



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$

**In case of Sentinel-1 data : reference not at mid range  
(Confirming previous observations made by Aresys)**

- Intra-pulse motion during pulse duration:

$$\tau \rightarrow \tau - \frac{f_{\text{DC}}}{K_r}$$

**based on theoretical considerations**





# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$

**In case of Sentinel-1 data : reference not at mid range  
(Confirming previous observations made by Aresys)**

- Intra-pulse motion during pulse duration:

$$\tau \rightarrow \tau + \frac{f_{\text{DC}}}{K_r}$$

**opposite sign of correction in case of Sentinel-1 data (to be clarified)**



# Correction for Satellite Motion Effects

- Inter-pulse motion from pulse transmission to echo reception (approximately):

$$t \rightarrow t - \tau_{\text{ref}}/2$$

**Already done in SAR processor.**

- Intra-pulse motion during echo reception:

$$t \rightarrow t - (\tau - \tau_{\text{ref}})/2$$

**In case of Sentinel-1 data : reference not at mid range  
(Confirming previous observations made by Aresys)**

- Intra-pulse motion during pulse duration:

$$\tau \rightarrow \tau + \frac{f_{\text{DC}}}{K_r}$$

**opposite sign of correction in case of Sentinel-1 data (to be clarified)**

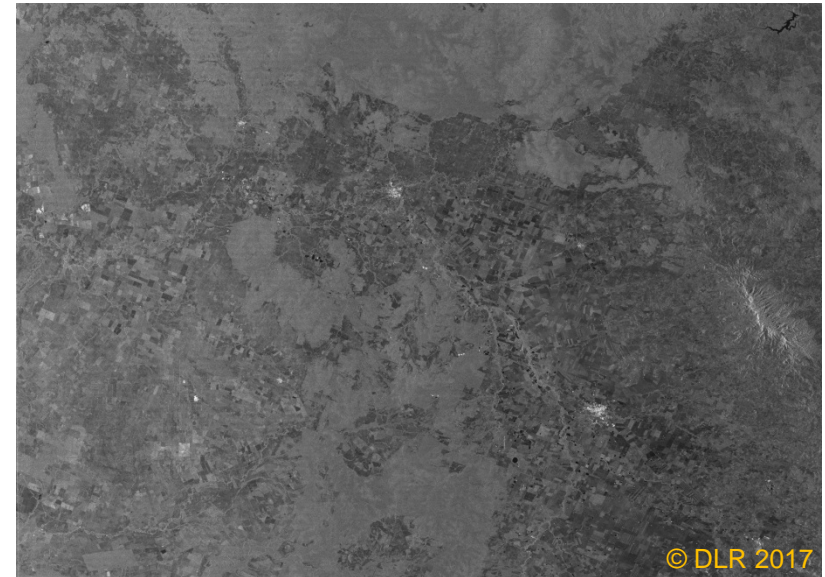
- Inter-pulse motion: Increase of signal travel distance:

$$\tau \rightarrow \tau \cdot \sqrt{1 - v_{\text{sat}}^2/c^2}$$



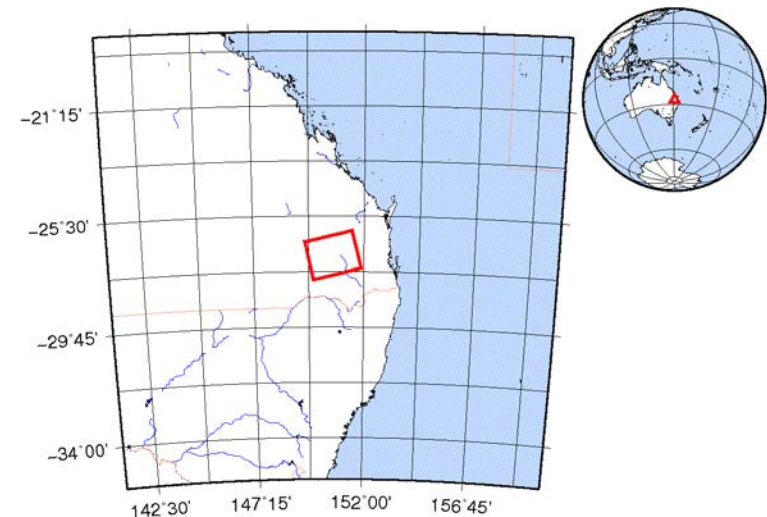
# Surat Basin Test Site

- Located at **Surat Basin, Queensland, Australia**
- Operated by **Geoscience Australia (GA)**
- **40 CRs** with known reference coordinates from on-site survey (by GA)
- Regularly imaged by **Sentinel-1** in **IW** mode
- Imaged by **TerraSAR-X** in **SM, SC** and **Wide SC** mode



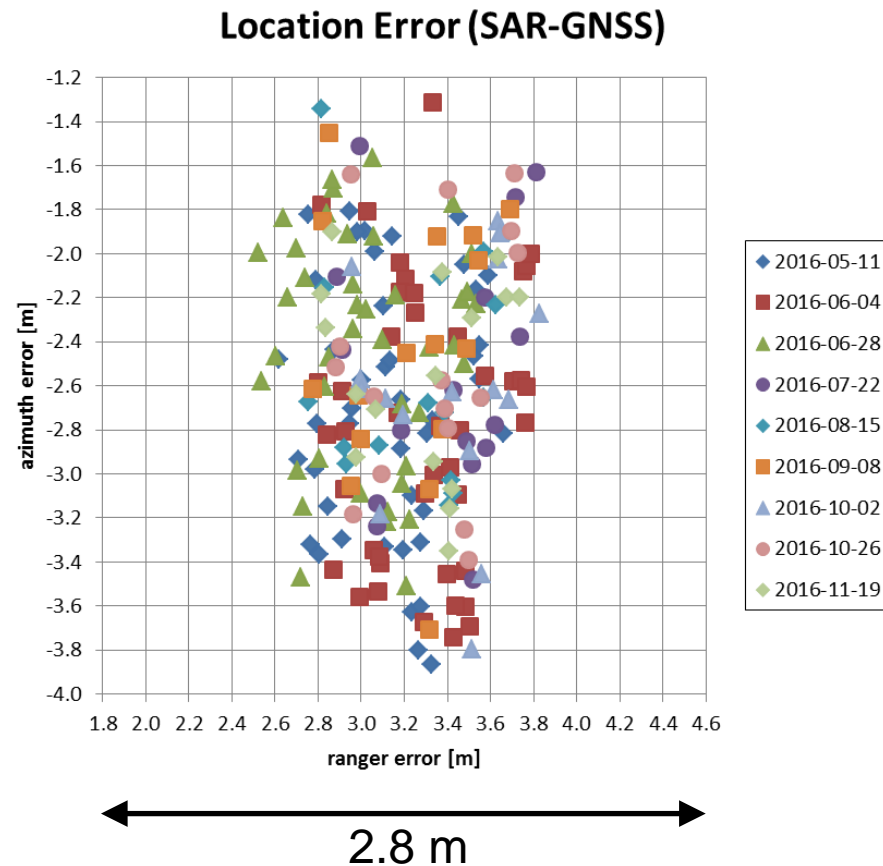
## • See also (at CEOS Workshop 2017):

- **Medhavy Thankappan et al.:**  
*“Calibration of Sentinel-1 and TerraSAR-X time-series SAR data over the Queensland Corner Reflector Array, Australia”*
- **Christoph Gisinger et al.:**  
*“The limits of spaceborne SAR geolocation: Can we attain the 1 cm level?”*



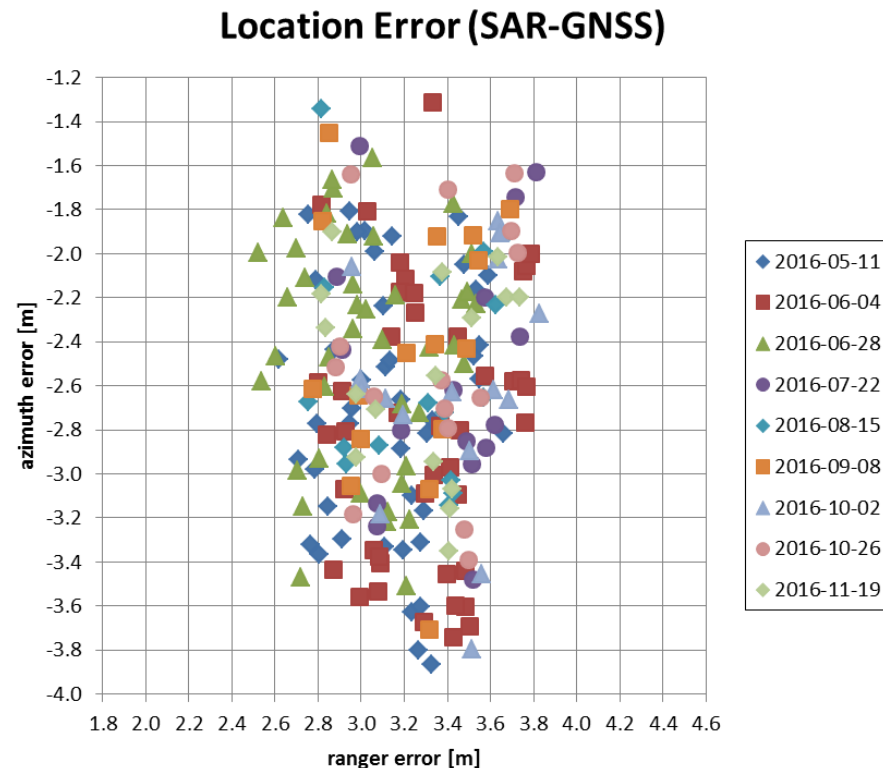
# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
  - ~~Signal propagation delays~~
  - ~~Solid earth tides~~
  - **Inter-pulse motion (by IPF)**
  - ~~Intra-pulse motion:~~
    - ~~Azimuth effect~~
    - ~~Range effect~~
- Location Error (SAR-GNSS):
  - Azimuth: -260 ± 57 cm
  - Range: +322 ± 31 cm



# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
  - ~~Signal propagation delays~~
  - ~~Solid earth tides~~
  - Inter-pulse motion (by IPF)
  - ~~Intra-pulse motion:~~
    - ~~Azimuth effect~~
    - ~~Range effect~~
- Location Error (SAR-GNSS):
  - Azimuth: -260 ± 57 cm
  - Range: +322 ± 31 cm



+1.8 m ←————→ +4.6 m  
2.8 m

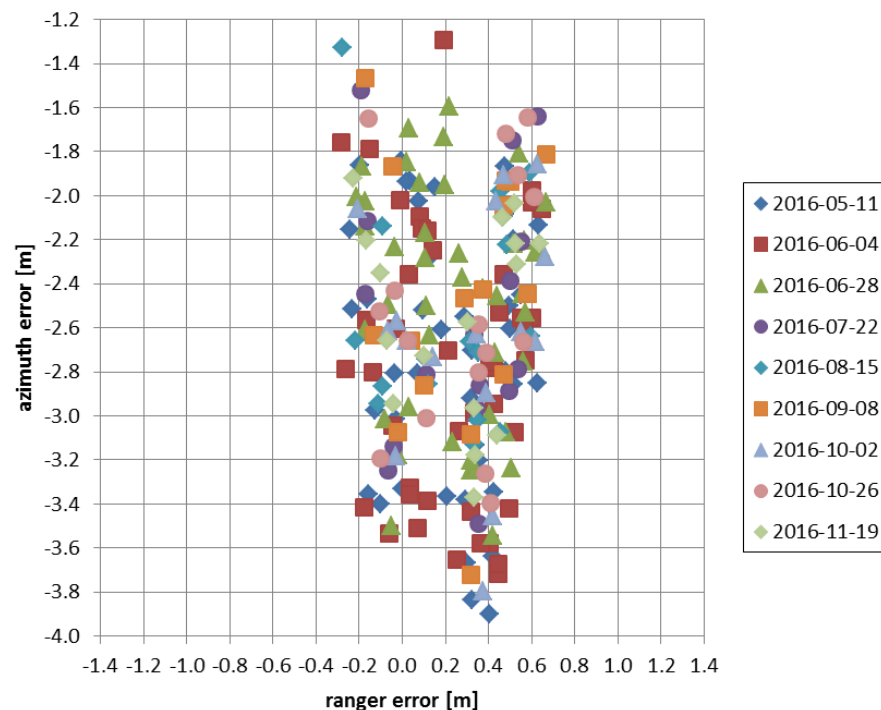




# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
    - **Signal propagation delays**
    - **Solid earth tides**
    - **Inter-pulse motion (by IPF)**
    - ~~Intra-pulse motion:~~
      - ~~Azimuth effect~~
      - ~~Range effect~~
  - Location Error (SAR-GNSS):
    - Azimuth:  $-261 \pm 57$  cm
    - Range:  $+24.0$   $\pm 26.8$  cm
- Range bias almost removed  
 • Range standard deviation lowered by about 4 cm

Location Error (SAR-GNSS)

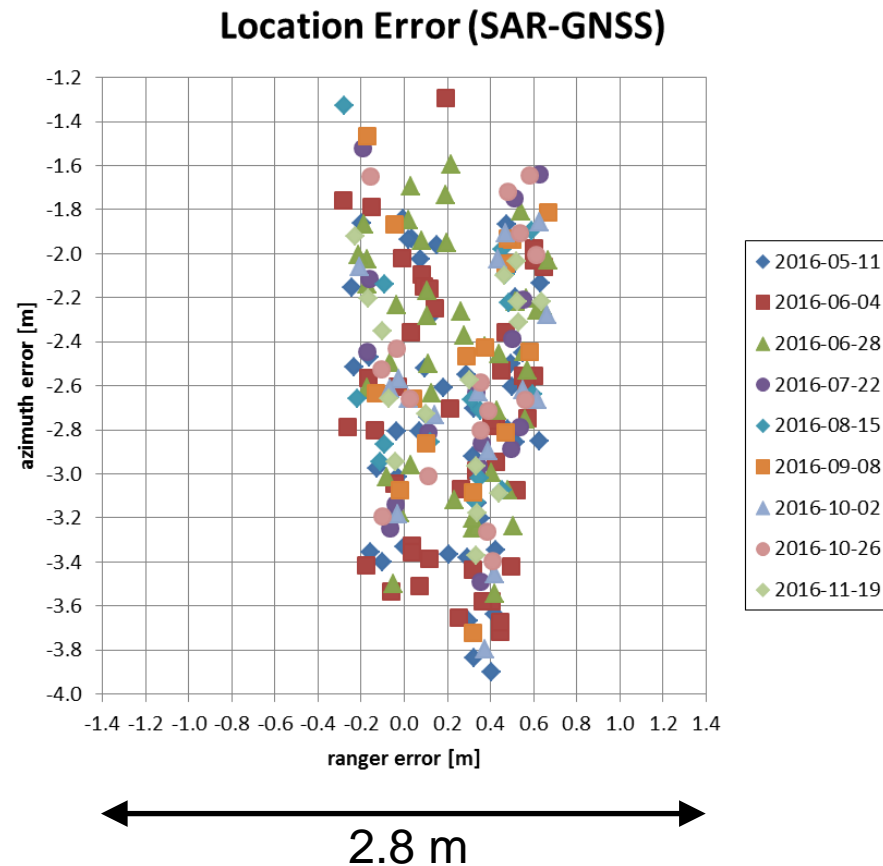


-1.4 m ← → +1.4 m  
 2.8 m



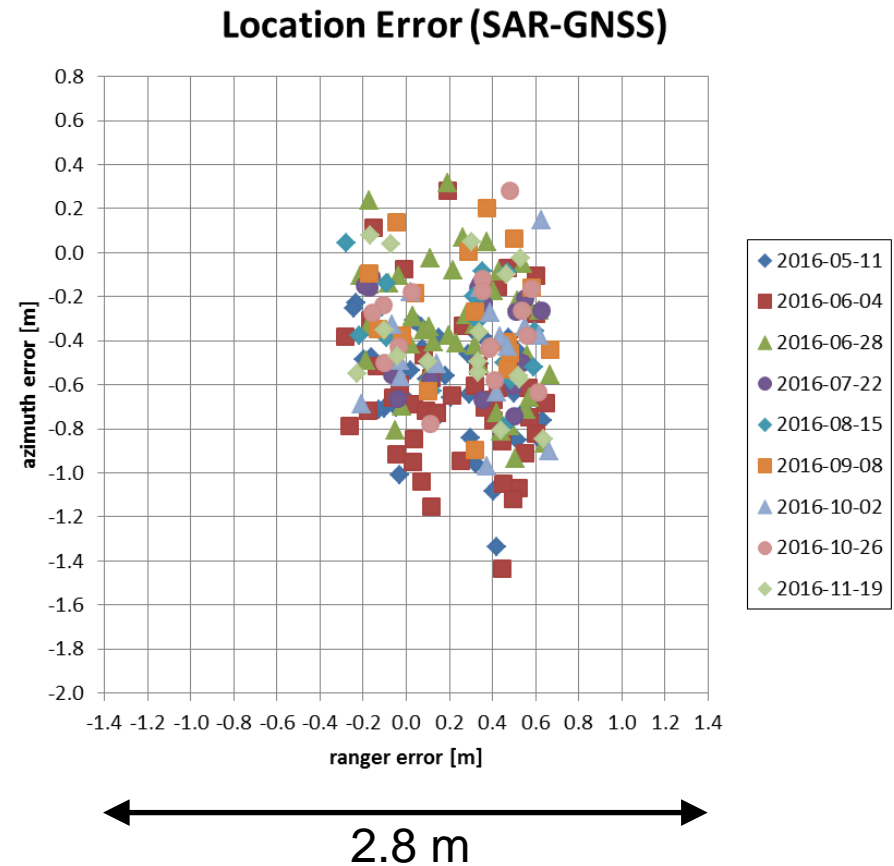
# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - Inter-pulse motion (by IPF)
  - ~~Intra-pulse motion:~~
    - ~~Azimuth effect~~
    - ~~Range effect~~
- Location Error (SAR-GNSS):
  - Azimuth: **-261 ± 57 cm**
  - Range: **+24.0 ± 26.8 cm**



# Localization Accuracy of Sentinel-1 IW Mode

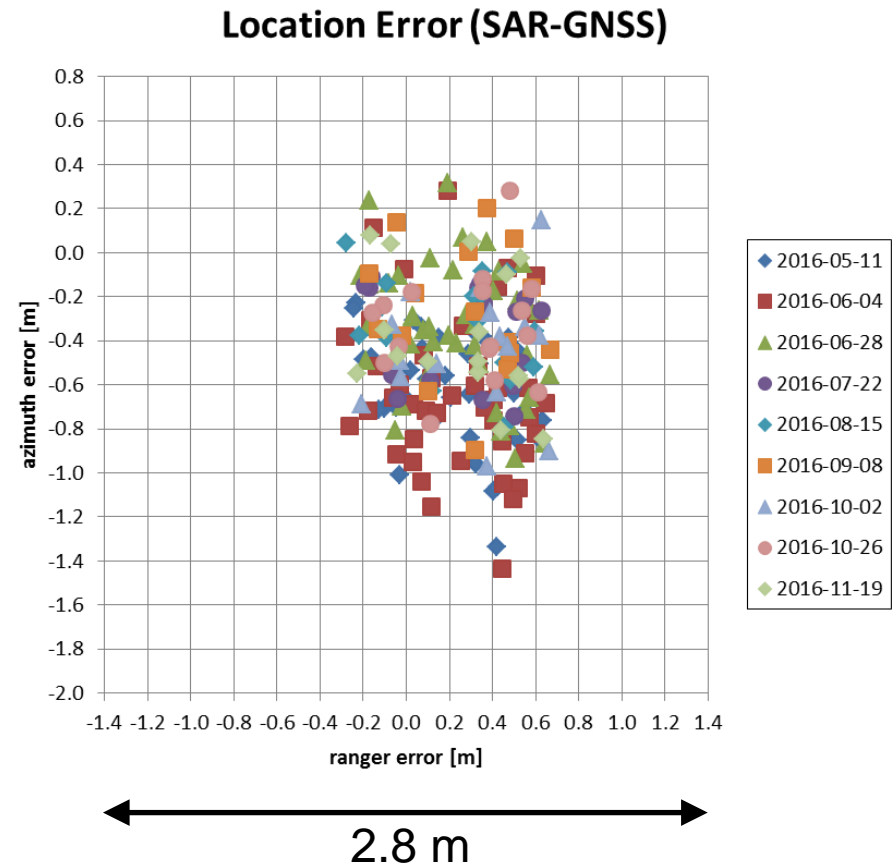
- Corrected:
    - Signal propagation delays
    - Solid earth tides
    - Inter-pulse motion (by IPF)
    - **Intra-pulse motion:**
      - **Azimuth effect**
      - ~~Range effect~~
  - Location Error (SAR-GNSS):
    - Azimuth: **-46 ± 31** cm
    - Range: **+24.0 ± 26.8** cm
- Most of azimuth bias removed
  - Azimuth standard deviation lowered by 26 cm





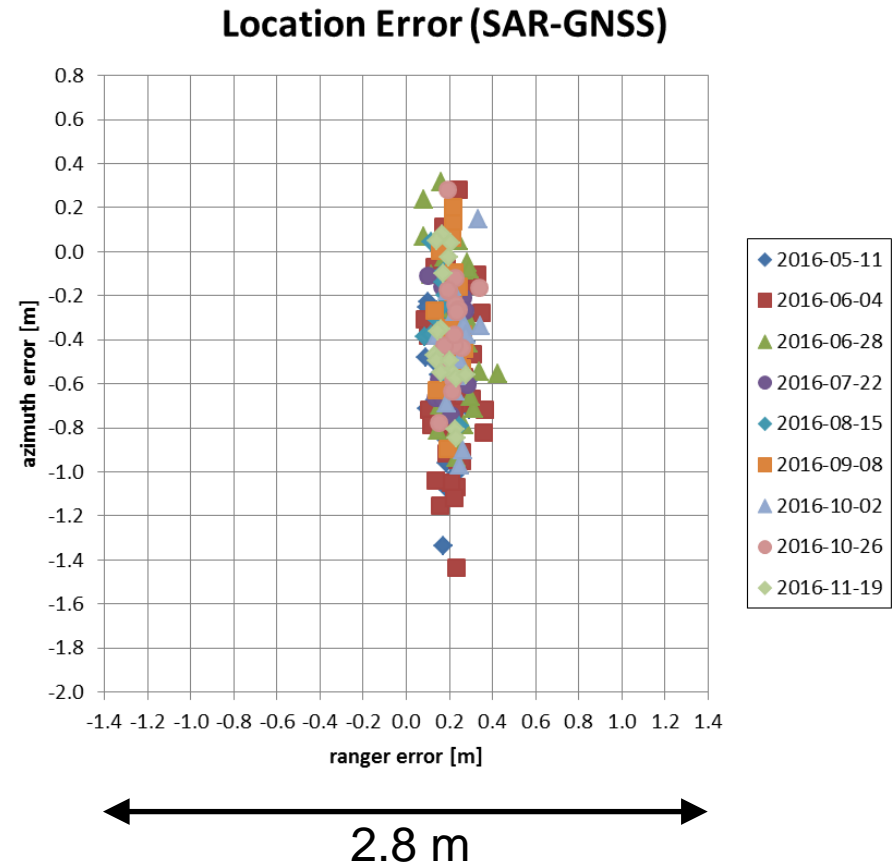
# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - Inter-pulse motion (by IPF)
  - **Intra-pulse motion:**
    - Azimuth effect
    - ~~Range effect~~
- Location Error (SAR-GNSS):
  - Azimuth:  $-46 \pm 31$  cm
  - Range:  $+24.0 \pm \underline{26.8}$  cm



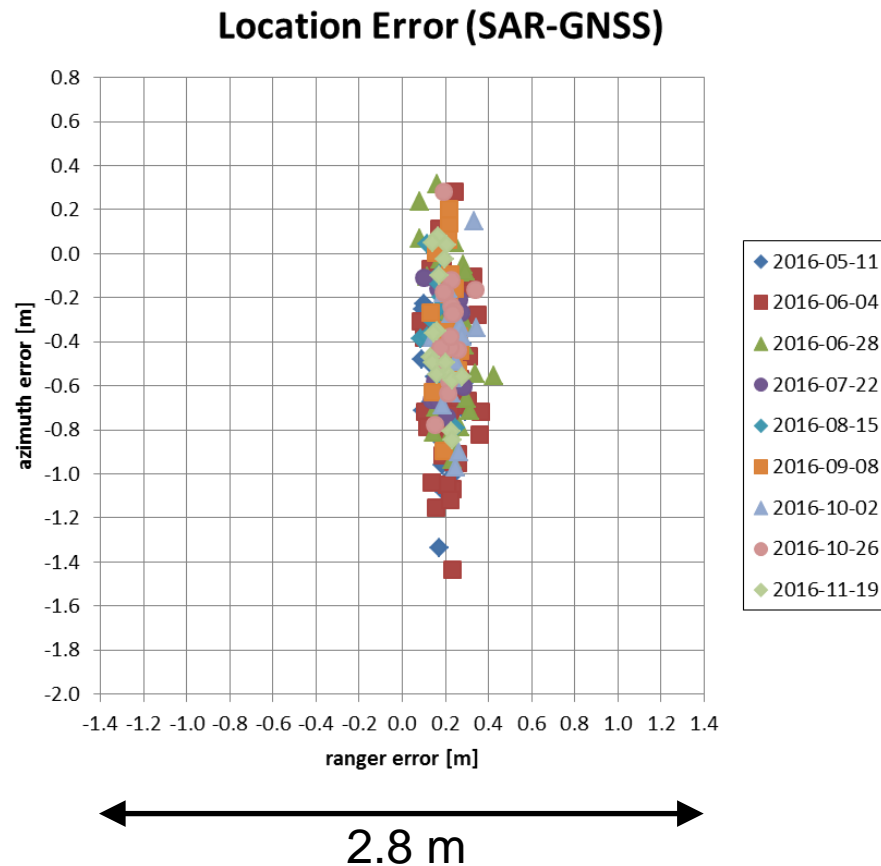
# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
    - Signal propagation delays
    - Solid earth tides
    - Inter-pulse motion (by IPF)
    - **Intra-pulse motion:**
      - Azimuth effect
      - **Range effect**
  - Location Error (SAR-GNSS):
    - Azimuth:  $-46 \pm 31$  cm
    - Range:  $+20.9 \pm \underline{5.7}$  cm
- Range bias lowered by about 3 cm  
 • Range standard deviation drastically lowered (almost by factor 5).



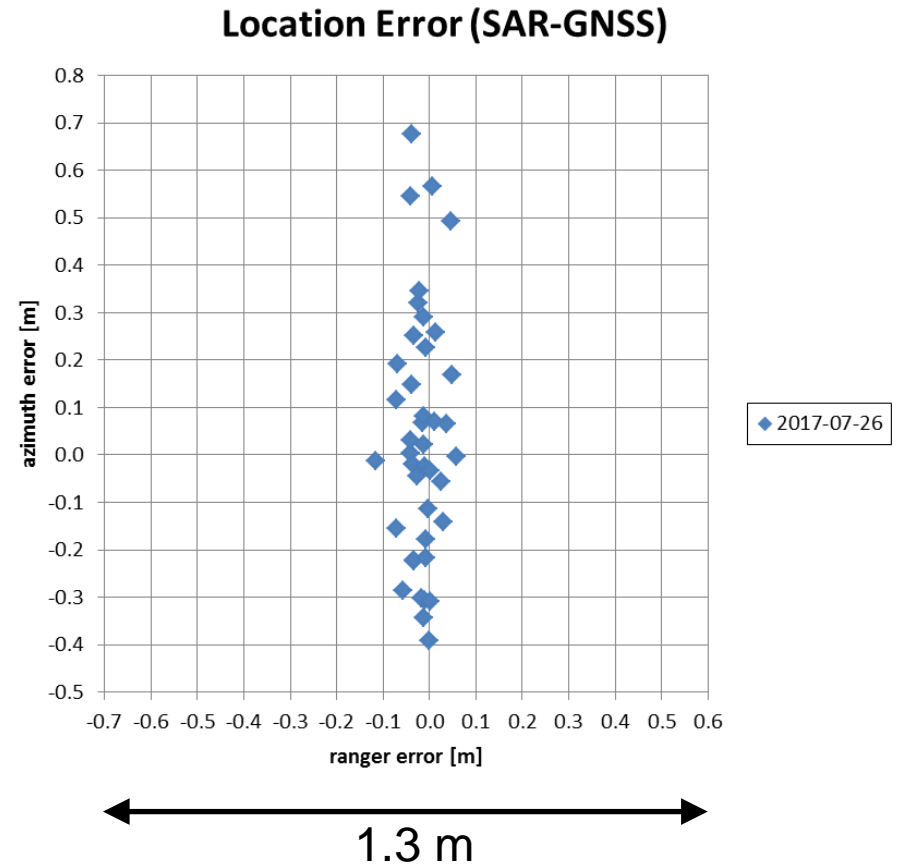
# Localization Accuracy of Sentinel-1 IW Mode

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - Inter-pulse motion (by IPF)
  - Intra-pulse motion:
    - Azimuth effect
    - Range effect
- Location Error (SAR-GNSS):
  - Azimuth: **-46**  $\pm$  31 cm
  - Range: **+20.9**  $\pm$  5.7 cm
- Recommendation:
  - Biases shall be corrected by instrument recalibration



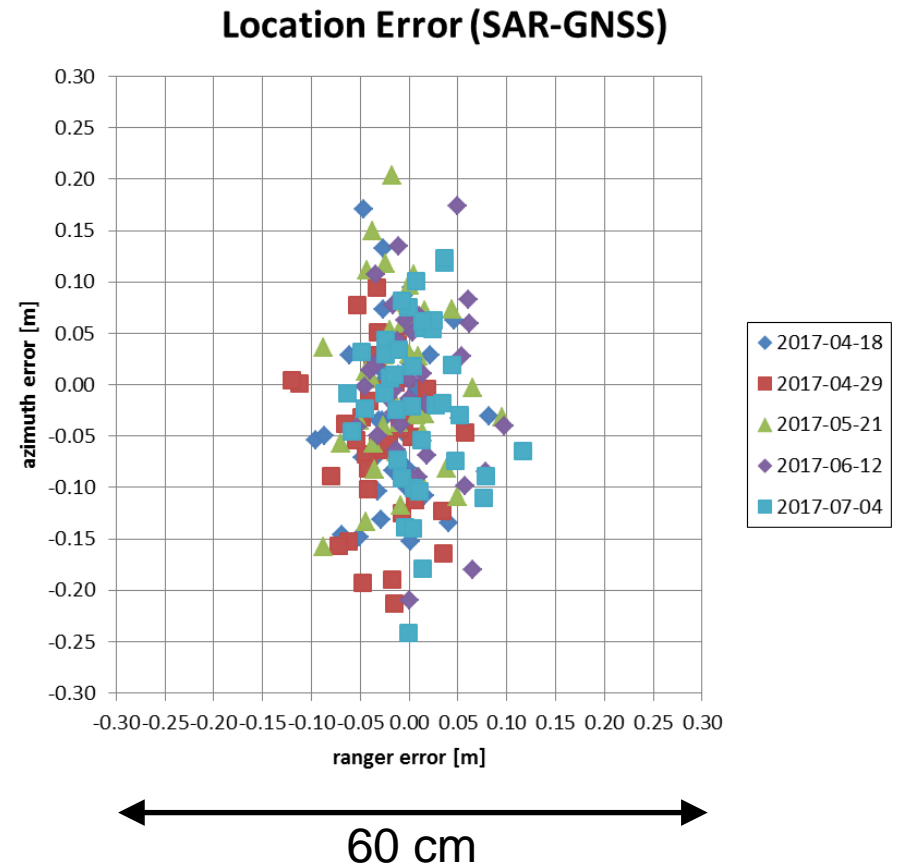
# Localization Accuracy of TerraSAR-X Wide ScanSAR Mode

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - **Inter-pulse motion (by TMSP)**
  - **Intra-pulse motion:**
    - **Azimuth effect (by TMSP)**
    - **Range effect (by TMSP)**
- Location Error (SAR-GNSS):
  - Azimuth:  $+3.8 \pm 26$  cm
  - Range:  $-1.6 \pm 3.5$  cm



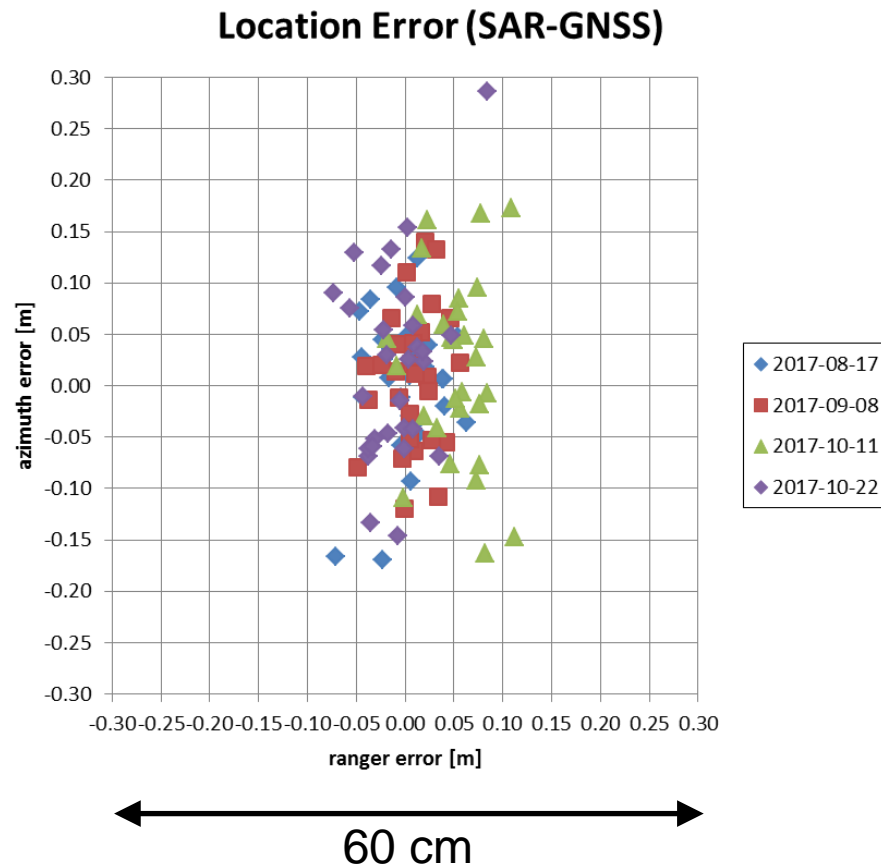
# Localization Accuracy of TerraSAR-X ScanSAR Mode (Eastern Part of Surat Basin)

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - Inter-pulse motion (by TMSP)
  - Intra-pulse motion:
    - Azimuth effect (by TMSP)
    - Range effect (by TMSP)
- Location Error (SAR-GNSS):
  - Azimuth:  $-2.1 \pm 8.0$  cm
  - Range:  $-0.8 \pm 3.8$  cm



# Localization Accuracy of TerraSAR-X ScanSAR Mode (Western Part of Surat Basin)

- Corrected:
  - Signal propagation delays
  - Solid earth tides
  - Inter-pulse motion (by TMSP)
  - Intra-pulse motion:
    - Azimuth effect (by TMSP)
    - Range effect (by TMSP)
- Location Error (SAR-GNSS):
  - Azimuth:  $+1.1 \pm 8.0$  cm
  - Range:  $+1.2 \pm 3.9$  cm



# Conclusions

- Stop-Go-Approximation is challenged when location accuracy at centimeter level is required.





# Conclusions

- Stop-Go-Approximation is challenged when location accuracy at centimeter level is required.
- Effects of inter-pulse and intra-pulse satellite motion have to be compensated for.





# Conclusions

- Stop-Go-Approximation is challenged when location accuracy at centimeter level is required.
- Effects of inter-pulse and intra-pulse satellite motion have to be compensated for.
- Recommendation w.r.t. future SAR missions:
  - It is most adequate to correction for these effects already during SAR processing.



# Conclusions

- Stop-Go-Approximation is challenged when location accuracy at centimeter level is required.
- Effects of inter-pulse and intra-pulse satellite motion have to be compensated for.
- Recommendation w.r.t. future SAR missions:
  - It is most adequate to correction for these effects already during SAR processing.
- If this is not applicable (in ongoing SAR mission):
  - Users need clear instructions to perform these corrections by post-processing of their location measurement results.



# Conclusions

- Stop-Go-Approximation is challenged when location accuracy at centimeter level is required.
- Effects of inter-pulse and intra-pulse satellite motion have to be compensated for.
- Recommendation w.r.t. future SAR missions:
  - It is most adequate to correction for these effects already during SAR processing.
- If this is not applicable (in ongoing SAR mission):
  - Users need clear instructions to perform these corrections by post-processing of their location measurement results.
- Improvements of inter-pulse and intra-pulse motion corrections are demonstrated based on example datatakes from the Sentinel-1 mission.





*Thank You for Your Attention!*



*This work is founded by ESA ESRIN within  
the framework of the FRM4SAR project  
(ESA Contract No. 4000119113/16/I-EF).*